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Comparison between CPBPV, ESC/Java, CBMC, Blast, EUREKA and Why for Bounded Program Verification

Hélène Collavizza¹, Michel Rueher¹, Pascal Van Hentenryck²

¹ Université de Nice-Sophia Antipolis, France ({[helen,rueher](mailto:helen.rueher@polytech.unice.fr)}@polytech.unice.fr)

² Brown University, Box 1910, Providence, RI 02912 (pvh@cs.brown.edu)

1 Abstract

This report describes experimental results for a set of benchmarks on program verification. It compares the capabilities of CPBVP “*Constraint Programming framework for Bounded Program Verification*” [4] with the following frameworks: ESC/Java, CBMC, Blast, EUREKA and Why.

2 Introduction

This report describes experimental results for a set of benchmarks on program verification. It compares the capabilities of CPBVP “*Constraint Programming framework for Bounded Program Verification*” [4] with the following frameworks:

- ESC/Java (<http://kind.ucd.ie/products/opensource/ESCJava2/>): Extended Static Checker for Java is a programming tool that attempts to find common run-time errors in JML-annotated Java programs by static analysis of the program code and its formal annotations.
- CBMC (<http://www.cprover.org/cbmc/>): is a Bounded Model Checker for ANSI-C and C++ programs. It allows verifying array bounds (buffer overflows), pointer safety, exceptions and user-specified assertions.
- Blast(<http://mtc.epfl.ch/software-tools/blast/>): Berkeley Lazy Abstraction Software Verification Tool is a software model checker for C programs.
- EUREKA (<http://www.ai-lab.it/eureka/>): is a C bounded model checker which uses an SMT solver instead of an SAT solver.
- Why (<http://why.lri.fr/>): is a software verification platform which integrates many existing provers (proof assistants such as Coq, PVS, HOL 4,... and decision procedures such as Simplify, Yices, ...).

All experiments were performed on the same machine, an Intel(R) Pentium(R) M processor 1.86GHz with 1.5G of memory, using the version of the verifiers that can be downloaded from their web sites (except for EUREKA project, for which we report the execution times given by the authors in [1] and [2]).

For each benchmark program, we describe the data entries and the verification parameters. Since the input formats slightly differ from one framework to another, we also give the input files that were used to perform the comparisons for each benchmark and each framework. In experimental result tables, UNABLE means that the framework is unable to validate the program (either because a lack of expression power or time overflow), NOT_FOUND that it doesn't detect an error that was inserted in the program, and FALSE_ERROR that it finds an error in a correct program.

3 Triangle classification

The *tritype* program is a standard benchmark in test case generation and program verification since it contains numerous non-feasible paths: only 10 paths correspond to actual inputs because of complex conditional statements in the program. The program takes three positive integers as inputs (the triangle sides) and returns 2 if the inputs correspond to an isoscele triangle, 3 if they correspond to an equilateral triangle, 1 if they correspond to some other triangle, and 4 otherwise (see 3.1).

3.1 Program used for CPBPV, ESC/Java and Why

```

/** Triangle classification
 * returns 4 if (i,j,k) are not the sides of a triangle
 * 3 if (i,j,k) is an equilateral triangle
 * 2 if (i,j,k) is an isoscele triangle
 * 1 if (i,j,k) is a scalene triangle
 */

/*@ requires (i >= 0 && j >= 0 && k >= 0);
   @ ensures
   @   (((i+j) <= k || (j+k) <= i || (i+k) <= j) ==> (\result == 4))
   @   && (((i+j) <= k || (j+k) <= i || (i+k) <= j) && (i==j && j==k)) ==> (\result == 3))
   @   && (((i+j) <= k || (j+k) <= i || (i+k) <= j) && !(i==j && j==k) && (i==j || j==k || i==k)) ==> (\result == 2))
   @   && (((i+j) <= k || (j+k) <= i || (i+k) <= j) && !(i==j && j==k) && !(i==j || j==k || i==k)) ==> (\result == 1));
   @*/
1 int tritype (int i, int j, int k) {
2   int trityp;
3   if (i == 0 || j == 0 || k == 0) {
4     trityp = 4;}
5   else {
6     trityp = 0;
7     if (i == j) {trityp = trityp + 1;}
8     if (i == k) {trityp = trityp + 2;}
9     if (j == k) {trityp = trityp + 3;}
10    if (trityp == 0) {
11      if ((i+j) <= k || (j+k) <= i || (i+k) <= j) {
12        trityp = 4;}
13      else {trityp = 1;}
14    }
15    else {
16      if (trityp > 3) {trityp = 3;}
17      else {
18        if (trityp == 1 && (i+j) > k) {
19          trityp = 2;}
20        else {
21          if (trityp == 2 && (i+k) > j) {
22            trityp = 2;}

```

```

23         else {
24             if (trityp == 3 && (j+k) > i) {
25                 trityp = 2;}
26             else {
27                 trityp = 4;}
28         }
29     }
30 }
31 }
32 }
33 return trityp;
34 }

```

3.2 C program used for CBMC

The only difference with the Java version is that we translated the “implies” statement of JML specification with the corresponding disjunction (ie $a \Rightarrow b$ is translated as $\neg a \vee b$).

```

int tritype(int i, int j, int k) {
    // PRECONDITION
    __CPROVER_assume(i>=0&&j>=0&&k>=0);
    int trityp ;
    if ( ( i <= 0) || ( j <= 0) || (k <= 0)){
        trityp = 4 ;
    }
    else {
        trityp = 0 ;
        if (i == j) trityp = trityp + 1 ;
        if (i == k) trityp = trityp + 2 ;
        if (j == k) trityp = trityp + 3 ;
        if (trityp == 0){
            if ( (i+j <= k) || (j+k <= i) || (i+k <= j)) {
                trityp = 4 ;
            }
            else{
                trityp = 1 ;
            }
        }
        else {
            if (trityp > 3) {
                trityp = 3 ;
            }
            else
                if ( (trityp == 1) && (i+j > k) ){
                    trityp = 2 ;
                }
            else
                if ( (trityp == 2) && (i+k > j) ){//ERROR trityp==1
                    trityp = 2 ;
                }
            else
                if ( (trityp == 3) && (j+k > i)) {
                    trityp = 2 ;
                }
            else {
                trityp = 4 ;
            }
        }
    }
}

// POSTCONDITION
assert(((i+j<=k)|| (j+k<=i)|| (i+k<=j)) || trityp == 4) &&
(!(((i+j<=k)|| (j+k<=i)|| (i+k<=j))&&((i==j)&&(j==k)))
|| trityp == 3) &&
(!(((i+j<=k)|| (j+k<=i)|| (i+k<=j))&&((i==j)&&(j==k)))

```

```

    &&((i==j)|| (j==k)|| (i==k))) || trityp == 2) &&
    (!( (i+j<=k)|| (j+k<=i)|| (i+k<=j))&&!( (i==j)&&(j==k))
    && !( (i==j)|| (j==k)|| (i==k))) || trityp == 1));

    return trityp ;
}

```

3.3 C program used for Blast

Blast is unable to deal with arithmetic expressions like $i+k \leq j$ unless these expressions have been collected as decisions taken in a program path. For example, assertion in line 22 (see program below), can be verified because it directly results from the “if” statement on line 15. But assertion in line 34 can’t be verified because it requires a reasoning on arithmetic expressions. So we used a slightly different version of the tritype program for Blast.

```

#include <assert.h>

int main(int i, int j, int k) {
1   int trityp ;
2   if ((i <= 0) || (j <= 0) || (k <= 0)){
3       trityp = 4 ;
4       assert((i <= 0) || (j <= 0) || (k <= 0));
5   }
6   else {
7       trityp = 0 ;
8       if (i == j)
9           trityp = trityp + 1 ;
10      if (i == k)
11          trityp = trityp + 2 ;
12      if (j == k )
13          trityp = trityp + 3 ;
14      if (trityp == 0) {
15          if ((i+j <= k) || (j+k <= i) || (i+k <= j)) {
16              trityp = 4 ;
17              assert((i+j<=k)|| (j+k<=i)|| (i+k<=j));
18          }
19          else{
20              trityp = 1 ;
21              assert((i!=j) && (j!=k) && (i!=k)
22                  && !( (i+j<=k)|| (j+k<=i)|| (i+k<=j)) ) );
23          }
24      }
25      else {
26          if (trityp > 3) {
27              trityp = 3 ;
28              assert((i==j && j==k && i==k));
29          }
30          else
31              if ((trityp == 1) && (i+j > k) ){
32                  trityp = 2 ;
33                  assert(i==j );
34                  //assert(!( (i+j<=k)|| (j+k<=i)|| (i+k<=j)));
35              }
36          else
37              if ((trityp == 2) && (i+k > j) ){ //ERROR trityp==1
38                  trityp = 2 ;
39                  assert(i==k );
40              }
41          else
42              if ((trityp == 3) && (j+k > i)) {
43                  trityp = 2 ;
44                  assert(j==k);

```

	CPBPV	ESC/Java	CBMC	Why	BLAST	BLAST (easier version)
time	0.287s	1.828s	0.82s	8.85s	UNABLE	0.716s

Table 1. Comparison table for Tritype program

```

45         }
46         else {
47             trityp = 4 ;
48             assert((i+j<=k) || (j+k<=i) || (i+k<=j));
         }
    }
    return trityp ;
}

```

3.4 Comparative results

Table 1 shows experimental results for *Tritype* program using CPBPV, ESC/Java, CBMC, BLAST and Why frameworks. Note that BLAST was unable to validate this example because the current version does not handle linear arithmetic. But it succeeded in verifying the easier version presented in section 3.3 in 0.716s.

Note that our previous approach using constraint programming and Boolean abstraction to abstract the conditions, validated this benchmark in 8.52 seconds when integers were coded on 16 bits [3]. It also explored 92 spurious paths.

4 Triangle classification with an error

In this section, we consider an erroneous version of *Tritype* program where we have replaced the test “*if ((trityp==2) && (i+k>j))*” in line 22 (see section 3.1) with the test “*if ((trityp==1) && (i+k>j))*”.

Since the local variable *trityp* is equal to 2 when $i=k$, if $(i+k)>j$ we know that (i,j,k) are the sides of an isoscele triangle. In fact, the two other triangular inequalities $i+j > k$ and $j+k > i$ are trivial because $j>0$. But when *trityp*=1, $i=j$ and this erroneous version can answer that the triangle is isoscele while it may not be a triangle at all (the triangular inequality $i+j > k$ or $j+k > i$ may not be verified). For example, it will return 2 when $(i,j,k)=(1,1,2)$.

4.1 Program used for CPBPV, ESC/Java and Why

We show below the programs used for CPBPV, ESC/Java and Why. The program for Blast was modified in a similar way.

```

/* an error has been inserted line 21: trityp==1 instead of 2*/

/*@ requires (i >= 0 && j >= 0 && k >= 0);
   @ ensures
   @   (((i+j) <= k || (j+k) <= i || (i+k) <= j) ==> (\result == 4))
   @   && (((i+j) <= k || (j+k) <= i || (i+k) <= j) && (i==j && j==k)) ==> (\result == 3))
   @   && (((i+j) <= k || (j+k) <= i || (i+k) <= j) && !(i==j && j==k) && (i==j || j==k || i==k)) ==> (\result == 2))

```

```

@  && ((!(i+j) <= k || (j+k) <= i || (i+k) <= j) && !(i==j && j==k) && !(i==j || j==k || i==k)) ==> (\result == 1));
@*/

1  int tritypeK0 (int i, int j, int k) {
2      int trityp;
3      if (i == 0 || j == 0 || k == 0) {
4          trityp = 4;}
5      else {
6          trityp = 0;
7          if (i == j) {trityp = trityp + 1;}
8          if (i == k) {trityp = trityp + 2;}
9          if (j == k) {trityp = trityp + 3;}
10         if (trityp == 0) {
11             if ((i+j) <= k || (j+k) <= i || (i+k) <= j) {
12                 trityp = 4;}
13             else {trityp = 1;}
14         }
15     }
16     if (trityp > 3) {trityp = 3;}
17     else {
18         if (trityp == 1 && (i+j) > k) {
19             trityp = 2;}
20         else {
21             if (trityp == 1 && (i+k) > j) { //ERROR: trityp==1 instead of 2
22                 trityp = 2;}
23             else {
24                 if (trityp == 3 && (j+k) > i) {
25                     trityp = 2;}
26                 else {
27                     trityp = 4;}
28             }
29         }
30     }
31     return trityp;
32 }

```

4.2 Program used for CBMC

We show below the program used for CBMC. The main function was used to run the C program in order to verify that the program contains an error.

```

#include <assert.h>
#include <stdio.h>

int tritype(unsigned int i,unsigned int j,unsigned int k) {
    int trityp ;
    if ( ( i <= 0) || (j <= 0) || (k <= 0)){
        trityp = 4 ;
    }
    else {
        trityp = 0 ;
        if ( i == j)
            trityp = trityp + 1 ;
        if ( i == k)
            trityp = trityp + 2 ;
        if ( j == k )
            trityp = trityp + 3 ;
        if (trityp == 0) {
            if ((i+j <= k) || (j+k <= i) || (i+k <= j)) {
                trityp = 4 ;
            }
            else { trityp = 1 ; }
        }
    }
}

```

```

else {
  if (trityp > 3) {
    trityp = 3 ; }
  else
    if ((trityp == 1) && (i+j > k)){
      trityp = 2 ; }
    else
      if ((trityp == 1) && (i+k > j)){ // ERROR: trityp == 1 instead of 2
        trityp = 2 ; }
      else
        if ((trityp == 3) && (j+k > i)) {
          trityp = 2 ; }
        else {
          trityp = 4 ; }
    }
  }
  assert(((i+j<=k)|| (j+k<=i)|| (i+k<=j)) || trityp == 4) &&
  (!((i+j<=k)|| (j+k<=i)|| (i+k<=j))&&((i==j)&&(j==k)))
  || trityp == 3) &&
  (!((i+j<=k)|| (j+k<=i)|| (i+k<=j))&&!(i==j)&&(j==k))
  &&((i==j)|| (j==k)|| (i==k))) || trityp == 2) &&
  (!((i+j<=k)|| (j+k<=i)|| (i+k<=j))&&!(i==j)&&(j==k))
  && !(i==j)|| (j==k)|| (i==k))) || trityp == 1));
  return trityp ;
}

int main(void) {
  int t = tritype(1,1,2);
  printf("trityp %i\n",t);
  return 0;
}

```

4.3 Comparative results

Table 2 shows experimental results for the *erroneous* version of *Tritype* program for CPBPV, ESC/Java, CBMC, BLAST and Why. Execution times correspond to the time required to find the first error.

For frameworks that were able to find the error, we give in section 4.4 the error traces printed by the framework.

Remark on results with CBMC Note that for CBMC framework, CBMC is unable to detect the error but when running the C program for values $(i, j, k) = (1, 1, 2)$, the assertion verification mechanism of C detects that the assertion is violated.

If we use “CPROVER_assert” instead of “assert” (as recommended by D. Kroening when we have contacted him), then CBMC finds the error in the erroneous version of tritype. Nevertheless, if we also use this option in the correct version of the tritype program, then CBMC finds a false error. The reason seems to be that CBMC works using modulo arithmetic and so we must specify that there is no overflow. So, we also added the statement:

$$CPROVER_{assume}(i + j >= 0 \&\& j + k >= 0 \&\& k + i >= 0)'$$

which means that there is no overflow into the sums.

	CPBPV	ESC/Java	CBMC	WHY	BLAST	BLAST (easier version)
time	0.056s	1.853s	NOT_FOUND	NOT_FOUND	UNABLE	0.452s

Table 2. Comparison table for Tritype program with error

4.4 Error traces

We give here the execution traces of the three frameworks that were able to find the error.

CPBPV error trace

```
i_0[-2147483647:2147483646] : 1
j_0[-2147483647:2147483646] : 1
k_0[-2147483647:2147483646] : 2
trityp_0[-2147483647:2147483646] : 0
trityp_1[-2147483647:2147483646] : 0
trityp_2[-2147483647:2147483646] : 1
trityp_3[-2147483647:2147483646] : 2
```

The result is variable *trityp_3* which is equal to 2. The two sides *i* and *j* are equals but (*i,j,k*) doesn't represent a triangle because the triangular inequality is not verified (i.e $i+j=k$). So returned value must be 4 (part 1 of the JML specification).

ESC/Java error trace

```
TritypeK0.java:67: Warning: Postcondition possibly not established (Post)
    }
    ^
```

```
Associated declaration is "TritypeK0.java", line 12, col 5:
    @ ensures ...
```

```
Execution trace information:
Executed else branch in "TritypeK0.java", line 23, col 7.
Executed then branch in "TritypeK0.java", line 25, col 15.
Executed else branch in "TritypeK0.java", line 28, col 3.
Executed else branch in "TritypeK0.java", line 31, col 3.
Executed else branch in "TritypeK0.java", line 42, col 8.
Executed else branch in "TritypeK0.java", line 46, col 9.
Executed else branch in "TritypeK0.java", line 50, col 10.
Executed then branch in "TritypeK0.java", line 51, col 39.
Executed return in "TritypeK0.java", line 66, col 2.
```

```
Counterexample context:
(0 < k:18.32)
((2 * j:18.25) <= k:18.32)
(k:18.32 <= intLast)
(longFirst < intFirst)
(1000001 <= intLast)
(null <= max(LS))
(eClosedTime(elems) < alloc)
(VAllocTime(this) < alloc)
((intFirst + 1000001) <= 0)
(intLast < longLast)
(0 <= j:18.25)
(k:18.32 == 0) == tmp0!cor:20.6
null.LS == @true
(null <= max(LS))
```

```

typeof(j:18.25) <: T_int
((j:18.25 + k:18.32) > j:18.25) == @true
(0 + 1) == 1
(j:18.25 == 0) == tmp1!cor:20.6
typeof(k:18.32) <: T_int
typeof(this) <: T_TritypeK0
((j:18.25 + j:18.25) > k:18.32) == tmp4!cand:47.9
typeof(this) <: T_TritypeK0
trityp:19.6<7> == 2
T_bigint == T_long
tmp0!cor:20.23 == tmp0!cor:20.6
trityp:19.6<2> == 1
trityp:19.6<5> == 2
elems@pre == elems
j:18.25 == i:18.18
trityp:19.6<8> == 2
tmp5!cand:51.25 == @true
trityp:19.6 == 2
trityp:26.4 == 1
trityp:19.6<3> == 1
state@pre == state
trityp:19.6<6> == 2
tmp1!cor:20.13 == tmp1!cor:20.6
trityp:19.6<1> == 1
tmp5!cand:51.13 == @true
alloc@pre == alloc
tmp4!cand:47.21 == tmp4!cand:47.9
!typeof(this) <: T_void
!T_java.lang.Object <: T_java.io.Serializable
typeof(this) != T_void
bool$false != @true
tmp4!cand:47.9 != @true
ecThrow != ecReturn
1 != 0
k:18.32 != j:18.25
k:18.32 != 0
this != null
trityp:19.6<7> != 4
tmp0!cor:20.23 != @true
j:18.25 != 0
tmp1!cor:20.6 != @true

```

CBMC trace

Counterexample:

```

State 15 file bsearchAssertK0.c line 10 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::low=0 (00000000000000000000000000000000)
State 16 file bsearchAssertK0.c line 10 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::high=7 (00000000000000000000000000000111)
State 17 file bsearchAssertK0.c line 11 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::result=-1 (11111111111111111111111111111111)
State 18 file bsearchAssertK0.c line 13 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::1::middle=3 (000000000000000000000000000011)
State 21 file bsearchAssertK0.c line 17 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::high=2 (0000000000000000000000000000010)
State 25 file bsearchAssertK0.c line 13 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::1::middle=1 (000000000000000000000000000001)
State 29 file bsearchAssertK0.c line 15 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::high=0 (000000000000000000000000000000)
State 33 file bsearchAssertK0.c line 13 function binsearch thread 0
-----

```

```

    bsearchAssertK0::binsearch::1::1::middle=0 (00000000000000000000000000000000)
State 37 file bsearchAssertK0.c line 15 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::high=-1 (11111111111111111111111111111111)
Violated property:
  file bsearchAssertK0.c line 21 function binsearch
  assertion
    result != -1 && a[result] == x || result == -1 && a[0] != x && a[1] != x
    && a[2] != x && a[3] != x && a[4] != x && a[5] != x && a[6] != x && a[7] != x
VERIFICATION FAILED

```

Blast trace

```

Start trace
  XXX
0 :: 0:      FunctionCall(__BLAST_initialize_tritypeK0.i()) :: -1
  XXX
0 :: 0:      Block(Return(0);) :: -1
  XXX
-1 :: -1:    Skip :: 27
  XXX
27 :: 27:    Pred(i@main > 0) :: -1
  XXX
27 :: 27:    Pred(j@main > 0) :: -1
  XXX
27 :: 27:    Pred(k@main > 0) :: -1
  XXX
33 :: 33:    Block(trityp@main = 0;) :: 34
  XXX
34 :: 34:    Pred(i@main == j@main) :: -1
  XXX
35 :: 35:    Block(trityp@main = trityp@main + 1;) :: 36
  XXX
36 :: 36:    Pred(i@main != k@main) :: -1
  XXX
38 :: 38:    Pred(j@main != k@main) :: -1
  XXX
40 :: 40:    Pred(trityp@main != 0) :: -1
  XXX
54 :: 54:    Pred(trityp@main <= 3) :: -1
  XXX
59 :: 59:    Pred(trityp@main == 1) :: -1
  XXX
59 :: 59:    Pred(i@main + j@main <= k@main) :: -1
  XXX
65 :: 65:    Pred(trityp@main == 1) :: -1
  XXX
65 :: 65:    Pred(i@main + k@main > j@main) :: -1
  XXX
66 :: 66:    Block(trityp@main = 2;) :: 67
  XXX
67 :: 67:    Pred(i@main != k@main) :: -1
  XXX
67 :: 67:    FunctionCall(__assert_fail(__assertion@__assert_fail = "i==k",__file@__assert_fail = "tritypeK0.c",__line@
  XXX
77 :: 77:    FunctionCall(__blast_assert()) :: -1
  XXX
End trace

```

5 Binary search

In this section we consider the usual binary search program which determines if a value x is present in a sorted array tab (see 5.1 for a Java version of this program).

5.1 Java program used for CPBPV and ESC/Java

```

/*@ requires (\forall int i; (i >= 0 && i < tab.length -1); tab[i] <= tab[i+1]);
   @ ensures
   @ ((\result == -1) ==> (\forall int i; (i >= 0 && i < tab.length); tab[i] != x))
   @ && ((\result != -1) ==> (tab[\result] == x));
   @*/
int binarySearch (int[] tab, int x) {
    int index = -1;
    int m = 0;
    int l = 0;
    int u = tab.length -1;
    while (index == -1 && l <= u) {
        m = (l + u) / 2;
        if (tab[m] == x) {
            index = m;
        }
        else {
            if (tab[m] > x) {
                u = m - 1;
            }
            else {
                l = m + 1;
            }
        }
    }
    return index;
}
}

```

5.2 C program for an instance of length 8 used with CBMC

In order to express the *forall* statements of the JML specification inside the CBMC framework, we unfolded the conditions for fixed array lengths. The program below shows the preconditions and postconditions for an array of length 8. We proceeded in the same way for other array lengths.

```

int binsearch(int x) {
    int a[8];
    // PRECONDITION
    __CPROVER_assume(a[0] <= a[1] && a[1] <= a[2] && a[2] <= a[3] && a[3] <= a[4]
        && a[4] <= a[5] && a[5] <= a[6] && a[6] <= a[7]);

    signed low=0, high=7;
    int result=-1;
    while(result!=-1 && low<=high) {
        signed middle=(high+low)/2;
        if(a[middle]<x)
            high=middle-1;
        else if(a[middle]>x)
            low=middle+1;
        else // a[middle]==x !
            result= middle;
    }
    // POSTCONDITION
    assert((result!=-1 && a[result]==x) || (result==-1 && (a[0]!=x && a[1]!=x && a[2]!=x &&
        a[3]!=x && a[4]!=x && a[5]!=x && a[6]!=x && a[7]!=x)));
    return result;
}

```

5.3 Program with invariant used with Why

This version of the binary search is given as example in the Why distribution. It uses a loop invariant which allows Why to use induction when generating proof obligations.

```

/*@ axiom mean_1 : \forall int x, int y; x <= y => x <= (x+y)/2 <= y */

/* binary_search(t,n,v) search for element v in array t
   between index 0 and n-1
   array t is assumed sorted in increasing order
   returns an index i between 0 and n-1 where t[i] equals v,
   or -1 if no element of t is equal to v
*/

/*@ requires
   @ n >= 0 && \valid_range(t,0,n-1) &&
   @ \forall int k1, int k2; 0 <= k1 <= k2 <= n-1 => t[k1] <= t[k2]
   @ ensures
   @ (\result >= 0 && t[\result] == v) ||
   @ (\result == -1 && \forall int k; 0 <= k < n => t[k] != v)
   @*/
int binary_search(int* t, int n, int v) {
  int l = 0, u = n-1;
  /*@ invariant
   @ 0 <= l && u <= n-1 &&
   @ \forall int k; 0 <= k < n => t[k] == v => l <= k <= u
   @ variant u-l
   @*/
  while (l <= u) {
    int m = (l + u) / 2;
    if (t[m] < v) l = m + 1;
    else if (t[m] > v) u = m - 1;
    else return m;
  }
  return -1;
}

```

5.4 Comparative results

Table 3 reports comparative results for the binary search.

For ESC/Java framework, the number of loop unfolding must be given. Since the worst case complexity of binary search algorithm is $O(\log(n))$ where n is the array length, we set the parameter “Loop” to $\log(n) + 1$.

In a similar way, within the CBMC framework, an overestimate of the number of loop unfoldings is required (parameter “unwind”).

Note that CPBPV doesn’t require any additional information (neither invariant nor loop unfolding bound) because at any time the entrance condition of the loop is known. When performing symbolic execution, it selects a path, taking decisions for conditional expressions as “if (tab[m]==x)”. These decisions involve that the lower and upper bounds l and u are assigned with constant values.

The Why framework was very efficient to make the verification when an invariant is given as shown in subsection 5.3 but was unable to make it if no invariant is provided.

The CBMC framework was not able to do the verification for an instance of array of length 32 (it was interrupted after 6691,87s).

CPBPV	array length	8	16	32	64	128	256
	time	1.081s	1.69s	4.043s	17.009s	136.80s	1731.696s
CBMC	array length	8	16	32	64	128	256
	time	1.37s	1.43s	TIMEOUT (>6000s)	TIMEOUT	TIMEOUT	TIMEOUT
Why	with invariant	11.18s					
	without invariant	UNABLE					
ESC/Java	FALSE_ERROR						
BLAST	UNABLE						

Table 3. Comparison table for binary search

ESC/Java found a false error in this program. David Cok, a developer of ESC/Java we have contacted, has answered that we need to add some loop invariants in order to be able to perform the proof.

6 Binary search with error

We consider here an erroneous version of the binary search algorithm. We update the lower bound and the upper bound in the same way, whether the middle value is greater or less than the searched value (see line 15 in program below). We modified in the same way the binary search versions for CBMC and Why.

```

class BsearchK0 {
  /*@ requires (\forall int i; (i >= 0 && i < tab.length -1); tab[i] <= tab[i+1]);
   @ ensures
   @   ((\result == -1) ==> (\forall int i; (i >= 0 && i < tab.length); tab[i] != x))
   @   && ((\result != -1) ==> (tab[\result] == x));
   @*/
  int binarySearch (int[] tab, int x) {
1    int index = -1;
2    int m = 0;
3    int l = 0;
4    int u = tab.length -1;
5    while (index == -1 && l <= u) {
6      m = (l + u) / 2;
7      if (tab[m] == x) {
8        index = m;
9      }
10     else {
11       if (tab[m] > x) {
12         u = m - 1;
13       }
14       else {
15         u = m - 1; //ERROR: u = m - 1 instead of l = m + 1;
16       }
17     }
18   }
19   return index;
20 }
}

```

6.1 Comparative results

Table 4 shows experimental results for *binary search* program with *error* for CPBPV, ESC/Java, CBMC, and Why using an invariant.

	CPBPV	ESC/Java	CBMC	WHY with invariant
length 8	0.027s	1.21 s	unwind=4 1.38s	NOT_FOUND
length 16	0.037s	1.347 s	unwind=6 1.69s	NOT_FOUND
length 32	0.064s	1.792 s	unwind=7 7.62s	NOT_FOUND
length 64	0.115s	1.886 s	unwind=8 27.05s	NOT_FOUND
length 128	0.241s	1.964 s	unwind=9 189.20s	NOT_FOUND

Table 4. Comparison table for binary search with error

The Why framework was unable to perform this proof because 60% of the proof obligations remained unknown.

6.2 Error traces

We display here the error trace found with CPBPV for an array of length 8 and integers coded on 32 bits.

CPBPV error trace

```
Counter-example found
x_0[-2147483647:2147483646] : -2147483646
i_0[-2147483647:2147483646] : [-2147483647..2147483647]
i_0[-2147483647:2147483646] : [-2147483647..2147483647]
i_0[-2147483647:2147483646] : [-2147483647..2147483647]
i_0[-2147483647:2147483646] : [-2147483647..2147483647]
result_0[-2147483647:2147483646] : -1
milieu_0[-2147483647:2147483646] : 0
gauche_0[-2147483647:2147483646] : 0
droite_0[-2147483647:2147483646] : 7
milieu_1[-2147483647:2147483646] : 3
droite_1[-2147483647:2147483646] : 2
milieu_2[-2147483647:2147483646] : 1
droite_2[-2147483647:2147483646] : 0
milieu_3[-2147483647:2147483646] : 0
droite_3[-2147483647:2147483646] : -1
JMLResult_0[-2147483647:2147483646] : -1
tab_0[0][-2147483647:2147483646] : -2147483647
tab_0[1][-2147483647:2147483646] : -2147483647
tab_0[2][-2147483647:2147483646] : -2147483646
tab_0[3][-2147483647:2147483646] : -2147483645
tab_0[4][-2147483647:2147483646] : -2147483645
tab_0[5][-2147483647:2147483646] : -2147483645
tab_0[6][-2147483647:2147483646] : -2147483645
tab_0[7][-2147483647:2147483646] : -2147483645
```

ESC/Java error trace We display here the error trace found with ESC/Java for all the possible array lengths. Command line is: `escj -Loop 64.5 BsearchKO.java`

```
BsearchKO.java:32: Warning: Postcondition possibly not established (Post)
    }
    -
```

Associated declaration is "BsearchK0.java", line 8, col 5:

Execution trace information:

```

Reached top of loop after 0 iterations in "BsearchK0.java", line 17, col 2.
Executed else branch in "BsearchK0.java", line 22, col 8.
Executed else branch in "BsearchK0.java", line 26, col 9.
Reached top of loop after 1 iteration in "BsearchK0.java", line 17, col 2.
Executed return in "BsearchK0.java", line 31, col 2.

```

CBMC error trace We display here the error trace found with CBMC for an array of length 8 and parameter unwind sets to 6.

Counterexample:

```

State 1 file /usr/include/getopt.h line 59 thread 0
-----
    optarg=NULL

State 2 file /usr/include/getopt.h line 59 thread 0
-----
    optarg#str=NULL

State 3 file /usr/include/getopt.h line 73 thread 0
-----
    optind=0 (00000000000000000000000000000000)

State 4 file /usr/include/getopt.h line 78 thread 0
-----
    opterr=0 (00000000000000000000000000000000)

State 5 file /usr/include/getopt.h line 82 thread 0
-----
    optopt=0 (00000000000000000000000000000000)

State 6 file /usr/include/stdio.h line 142 thread 0
-----
    stdin=NULL

State 7 file /usr/include/stdio.h line 143 thread 0
-----
    stdout=NULL

State 8 file /usr/include/stdio.h line 144 thread 0
-----
    stderr=NULL

State 9 file <built-in> line 12 thread 0
-----
    __CPROVER_alloc=(assignment removed)

State 10 file <built-in> line 13 thread 0
-----
    __CPROVER_alloc_size=(assignment removed)

State 11 file /usr/include/bits/sys_errlist.h line 27 thread 0
-----
    sys_nerr=0 (00000000000000000000000000000000)

State 12 file /usr/include/unistd.h line 474 thread 0
-----
    __environ=NULL

State 15 file bsearchAssertK0.c line 10 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::low=0 (00000000000000000000000000000000)

State 16 file bsearchAssertK0.c line 10 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::high=7 (00000000000000000000000000000111)

State 17 file bsearchAssertK0.c line 11 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::result=-1 (11111111111111111111111111111111)

State 18 file bsearchAssertK0.c line 13 function binsearch thread 0
-----
    bsearchAssertK0::binsearch::1::1::middle=3 (00000000000000000000000000000111)

```



```

State 21 file bsearchAssertK0.c line 21 function binsearch thread 0
-----
bsearchAssertK0::binsearch::1::high=2 (00000000000000000000000000000010)

State 25 file bsearchAssertK0.c line 13 function binsearch thread 0
-----
bsearchAssertK0::binsearch::1::1::middle=1 (00000000000000000000000000000001)

State 29 file bsearchAssertK0.c line 15 function binsearch thread 0
-----
bsearchAssertK0::binsearch::1::high=0 (00000000000000000000000000000000)

State 33 file bsearchAssertK0.c line 13 function binsearch thread 0
-----
bsearchAssertK0::binsearch::1::1::middle=0 (00000000000000000000000000000000)

State 37 file bsearchAssertK0.c line 15 function binsearch thread 0
-----
bsearchAssertK0::binsearch::1::high=-1 (11111111111111111111111111111111)

Violated property:
file bsearchAssertK0.c line 21 function binsearch
assertion
result != -1 && a[result] == x || result == -1 && a[0] != x && a[1] != x && a[2] != x && a[3] != x && a[4] != x && a[5] != x

VERIFICATION FAILED

```

7 Bubble sort with initial condition

This example is taken from [1] and performs a bubble sort of an array t which contains integers from 0 to $t.length$ given in decreasing order. The *EUREKA* tool [1] validates the benchmark for arrays of lengths up to 8. In particular, it takes 91 seconds to verify for length 8.

7.1 Java program used for CPBPV and ESC/Java

```

/* Example taken from Mantovani et al [SPIN'2006]
 * bubble sort with a precondition
 */

class BubbleSortMantovani {
  /* @ requires (\forallall int i; 0<= i && i < tab.length; tab[i] = tab.length -1-i);
   * @ ensures (\forallall int i; 0<= i && i < tab.length-1; tab[i]<=tab[i+1]);
   */
  void tri(int[] tab) {
    int i=0;
    while (i<tab.length-1){
      int j=0;
      while (j < tab.length-i-1) {
        if (tab[j]>tab[j+1]) {
          int aux = tab[j];
          tab[j]= tab[j+1];
          tab[j+1] = aux;
        }
        j++;
      }
      i++;
    }
  }
}

```

	CPBPV	ESC/Java	CBMC	EUREKA
length 8	0.031s	3.778 s	1.11s	91s
length 16	0.032s	UNABLE	2.01s	UNABLE
length 32	UNABLE	UNABLE	6.10s	UNABLE
length 64	UNABLE	UNABLE	37.65s	UNABLE

Table 5. Comparison table for bubble sort

7.2 C program for an instance of length 8 used for CBMC

```

void bubble() {
  int a[8];
  // PRECOND
  __CPROVER_assume(a[0]==7 &&a[1]==6 &&a[2]==5 &&a[3]==4 &&a[4]==3 &&a[5]==2 &&a[6]==1 &&a[7]==0 );

  int i=0;
  while (i<7){
    int j=0;
    while (j < 7-i) {
      if (a[j]>a[j+1]) {
        int aux = a[j];
        a[j]= a[j+1];
        a[j+1] = aux;
      }
      j++;
    }
    i++;
  }
  // POSTCONDITION
  assert(a[0]<=a[1]&&a[1]<=a[2]&&a[2]<=a[3]&&a[3]<=a[4]&&a[4]<=a[5]&&a[5]<=a[6]
        &&a[6]<=a[7]);
}

```

7.3 Comparative results

Table 5 shows the experimental results for the bubble sort.

For the CPBPV framework, *UNABLE* corresponds to a memory capacity overflow. This is due to the need of SSA-like array renaming to express successive assignments. In this first prototype, we did not carefully manage the memory and so we duplicated indexes of the array which have not changed. This could easily be improved in a next version.

For ESC/Java framework, *UNABLE* corresponds to the message “Caution: Unable to check method tri(int[]) of type BubbleSortMantovani because its VC is too large”.

8 Sum of the square of the n first integers

This program computes the sum of the squares of the n first integers. The specification is that the sum is equal to $n \times (n + 1) \times (n \times 2 + 1)/6$. The main interest of this example is that it contains a non linear expression.

We didn’t perform the verification with EUREKA and BLAST, because they do not deal with non-linear expressions.

	CPBPV	CBMC	ESC/Java
length 8	0.152s	0.83s	FALSE_ERROR
length 16	0.557s	0.85s	FALSE_ERROR
length 32	1.111s	0.95s	FALSE_ERROR
length 64	1.144s	1.13s	FALSE_ERROR
length 128	1.868s	1.60s	FALSE_ERROR

Table 6. Comparison table for sum of squares

ESC/Java found a false error.

CBMC was able to verify this program only if we add a precondition which set n to a constant value.

Table 6 displays comparative results.

8.1 Java program used for CPBPV

```

/** sum of the square of the n first integers
 */
class SquareSum {

    /** requires (n >= 0);
     * ensures \result == (n*(n+1)*((n*2)+1))/6;
     */
    int somme (int n) {
        int i;
        int s = 0;
        while (i<=n) {
            s = s+i*i;
            i = i+1;
        }
        return s;
    }
}

```

8.2 C program used for CBMC

In order to be able to perform the proof, we had to insert a precondition which fixes the value of parameter n .

```

int somme (int n) {
    // PRECONDITION
    __CPROVER_assume(n==8);
    int i=0;
    int s = 0;
    while (i<=n) {
        s = s+i*i;
        i = i+1;
    }
    //POSTCONDITION
    assert(s==n*(n+1)*((n*2)+1)/6);
    return s;
}

```

9 Sum of the square of any permutation of the n first integers

This benchmark illustrates some capabilities of CPBPV framework that are not handled by other frameworks. It emphasizes the ability of specifying combinatorial constraints and of solving nonlinear problems. The `alldifferent` constraint[6] in the pre-condition specifies that all the elements of the array are different, while the program constraints and postcondition involves quadratic and cubic constraints.

This program takes two parameters as inputs: an array and its length. The array contains any permutation of the integers from 0 to n . It returns the sum of the squares of the array elements, which must be equal to $n \times (n+1) \times (2n+1)/6$.

```

/** Sum of the square of the n first integers
 * array t contains values between 0 and t.length-1 which are all different
 * (i.e array t contains any permutation of (0..t.length-1))
 */
class SquareSumArray {
/*
  @ requires (n == t.length-1) &&
  @   (\forall int i; 0<=i && i<t.length-1; 0<=t[i]&&t[i]<=n) &&
  @   \alldifferent t; // More compact notation than the JML quantified formulae
  @ ensures \result == n*(n+1)*(2*n+1)/6;
  @*/
1 int sum(int[] t, int n) {
2   int s = 0;
3   int i = 0;
4   while (i!=t.length) {
5     s=s+t[i]*t[i]
6     i =i+1;   }
7   return s;}

```

9.1 Experimental results

The maximum instance that we were able to solve with CPBPV framework was an array of size 10 in 66.179s.

10 Selection Sort

This last benchmark highlights both modular verification and the `element` constraint of constraint programming to index arrays with arbitrary expressions.

10.1 Selection sort for modular verification

```

/*@ ensures (\forall int i; 0<=i && i<t.length-1; t[i]<=t[i+1]) @*/
1 static void selectionSort(int[] t) {
2   for (int i=0; i<t.length;i++){
3     int k = findMin(t,i);
4     int tmp = t[i];
5     t[i]= t[k];
6     t[k] = tmp;   } }
/*@ requires 0<=l && l<t.length
  @ ensures (l<=\result) && (\result<t.length)
  @   && (\forall int k; l<=k && k<t.length; t[\result]<=t[k]) @*/
1 static int findMin(int[] t,int l) {

```

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```
2   int idx = 1;
3   for (int j = 1+1; j < t.length;j++)
4       if (t[idx]>t[j])
5           idx = j;
6   return idx; }
```

10.2 Modular verification and “element constraint”

Assume that function `findMin` has been verified for arbitrary integers. When encountering a call to `findMin`, CPBPV first checks if its precondition is entailed by the constraint store, which requires a consistency check of the constraint store with respect to the negation of the precondition. Then CPBPV replaces the call by the post-condition where the formal parameters are replaced by the actual variables. In particular, for the first iteration of the loop and an array length of 40, CPBPV generates the constraint

$$0 \leq k^0 < 40 \wedge t^0[k^0] \leq t^0[0] \wedge \dots \wedge t^0[k^0] \leq t^0[39].$$

This constraint is interesting, since it features `element` constraint [7], i.e., the ability of indexing arrays with expressions containing variables. Indeed, k^0 is a variable and a constraint like $t^0[k^0] \leq t^0[0]$ indexes the array t^0 of variables using k^0 . The `element` constraint is an important functionality of constraint programming, not only because of its ubiquity in practice but also because it highlights the kind of symbolic processing and filtering allowed by this technology. Note also that the subsequent assignments also create `element` constraints.

10.3 Comparative results

The modular verification of the selection sort explores only a single path, is independent of the integer representation, and takes less than 0.01s for arrays of size 40. The bottleneck in verifying selection sort is the validation of function `findMin`, which requires the exploration of many paths. However the complete validation of selection sort takes less than 4 seconds for an array of length 6. Once again, this should be contrasted with the model-checking approach of Eureka [1]. On a version of selection sort where all variables are assigned specific values (contrary to our verification which makes no assumptions on the inputs), Eureka takes 104 seconds on a faster machine. Reference [1] also reports that CBMC takes 432.6 seconds, that BLAST cannot solve this problem, and that SATABS [5] only verifies the program for an array with 2 elements.

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